

Trigonométrie

الحساب المثلثي

Formules principales		صيغ تحويل رئيسية
$\tan(a + b) = \frac{\tan a + \tan b}{1 - \tan a \tan b}$ $\tan(a - b) = \frac{\tan a - \tan b}{1 + \tan a \tan b}$	$\cos(a + b) = \cos a \cos b - \sin a \sin b$ $\cos(a - b) = \cos a \cos b + \sin a \sin b$	$\sin(a + b) = \sin a \cos b + \cos a \sin b$ $\sin(a - b) = \sin a \cos b - \cos a \sin b$
Dédutions		استنتاجات
$\tan(2x) = \frac{2 \tan x}{1 - \tan^2 x}$	$\cos(2x) = \cos^2 x - \sin^2 x$ $\cos(2x) = 2 \cos^2 x - 1$ $\cos(2x) = 1 - 2 \sin^2 x$	$\sin(2x) = 2 \sin x \cos x$
On pose :	$t = \tan(x/2)$	نضع:
$\tan x = \frac{2t}{1-t^2}$	$\cos x = \frac{1-t^2}{1+t^2}$	$\sin x = \frac{2t}{1+t^2}$
Passage du produit à la somme		تحويل الجداء الى مجموع
$\cos a \cos b = \frac{1}{2} [\cos(a + b) + \cos(a - b)]$ $\sin a \sin b = -\frac{1}{2} [\cos(a + b) - \cos(a - b)]$ $\sin a \cos b = \frac{1}{2} [\sin(a + b) + \sin(a - b)]$ $\cos a \sin b = \frac{1}{2} [\sin(a + b) - \sin(a - b)]$		
Passage de la somme au produit		تحويل المجموع الى الجداء
$\cos p + \cos q = 2 \cos\left(\frac{p+q}{2}\right) \cos\left(\frac{p-q}{2}\right)$ $\cos p - \cos q = -2 \sin\left(\frac{p+q}{2}\right) \sin\left(\frac{p-q}{2}\right)$ $\sin p + \sin q = 2 \sin\left(\frac{p+q}{2}\right) \cos\left(\frac{p-q}{2}\right)$ $\sin p - \sin q = 2 \cos\left(\frac{p+q}{2}\right) \sin\left(\frac{p-q}{2}\right)$		
Transformation de l'expression	$a \cos x + b \sin x$	تحويل الصيغة
$a \cos x + b \sin x = \sqrt{a^2 + b^2} \left[\frac{a}{\sqrt{a^2 + b^2}} \cos x + \frac{b}{\sqrt{a^2 + b^2}} \sin x \right]$ $a \cos x + b \sin x = \sqrt{a^2 + b^2} [\cos \alpha \cos x + \sin \alpha \sin x]$ $a \cos x + b \sin x = \sqrt{a^2 + b^2} \cos(x - \alpha)$		
<p>Avec: $\cos \alpha = \frac{a}{\sqrt{a^2 + b^2}}$ et $\sin \alpha = \frac{b}{\sqrt{a^2 + b^2}}$</p>		